



1. Let $F(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$. Then $F(\alpha) \cdot F(\alpha')$ is equal to

- (a) $F(\alpha\alpha')$ (b) $F(\alpha/\alpha')$ (c) $F(\alpha + \alpha')$ (d) $F(\alpha - \alpha')$

2. For the matrix $A = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 2 & 1 \\ 2 & 1 & 0 \end{bmatrix}$, which of the following is

correct

- (a) $A^3 + 3A^2 - I = 0$ (b) $A^3 - 3A^2 - I = 0$
(c) $A^3 + 2A^2 - I = 0$ (d) $A^3 - A^2 + I = 0$

3. If $A = \begin{bmatrix} 4 & 2 \\ 3 & 4 \end{bmatrix}$, then $|\text{adj} A|$ is equal to

- (a) 16 (b) 10 (c) 6 (d) None of these

4. The inverse of matrix $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ is

- (a) $\begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$ (b) $\frac{1}{ad-bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$,

- (c) $\frac{1}{|A|} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ (d) $\begin{bmatrix} b & -a \\ d & -c \end{bmatrix}$

5. Let $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$ and $10B = \begin{bmatrix} 4 & 2 & 2 \\ -5 & 0 & \alpha \\ 1 & -2 & 3 \end{bmatrix}$. If B is the

inverse of matrix A , then α is

- (a) 5 (b) -1 (c) 2 (d) -2

6. Matrix $A = \begin{bmatrix} 1 & 0 & -K \\ 2 & 1 & 3 \\ K & 0 & 1 \end{bmatrix}$ is invertible for

- (a) $K = 1$ (b) $K = -1$ (c) $K = 0$ (d) All real K

7. Let $f(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{bmatrix}$, where $\alpha \in \mathbb{R}$, then

$[f(\alpha)]^{-1}$ is equal to

- (a) $f(-\alpha)$ (b) $f(\alpha^{-1})$ (c) $f(2\alpha)$ (d) None

8. If I is a unit matrix of order 10, then the determinant of I is equal to

- (a) 10 (b) 1 (c) 1/10 (d) 9

9. If $A = \begin{bmatrix} \alpha & 2 \\ 2 & \alpha \end{bmatrix}$ and $|A^3| = 125$ then $\alpha =$

- (a) ± 3 (b) ± 2 (c) ± 5 (d) 0

10. If $|A|$ denotes the value of the determinant of the square matrix A of order 3, then $|-2A| =$

- (a) $-8|A|$ (b) $8|A|$ (c) $-2|A|$ (d) None of these

11. The system $AX = B$ of n equations in n unknowns has infinitely many solutions if

- (a) $\det A \neq 0$ (b) $\det A = 0, (\text{adj} A)B \neq 0$
(c) $\det A = 0, (\text{adj} A)B = 0$ (d) $\det A \neq 0, (\text{adj} A)B = 0$

12. If $A = \begin{bmatrix} -2 & 3 & -1 \\ -1 & 2 & -1 \\ -6 & 9 & -4 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 3 & -1 \\ 2 & 2 & -1 \\ 3 & 0 & -1 \end{bmatrix}$, then

- (a) $AB = BA$ (b) $AB \neq BA$
(c) $AB = \frac{1}{2}BA$ (d) None of these.

13. If $A = \begin{bmatrix} 1 & \tan x \\ -\tan x & 1 \end{bmatrix}$, then the value of $|A^T A^{-1}|$ is

- (a) $\cos 4x$ (b) $\sec^2 x$ (c) $-\cos 4x$ (d) 1

14. If $A = \begin{bmatrix} 2 & 3 & 4 \\ 5 & -3 & 8 \\ 9 & 2 & 16 \end{bmatrix}$, then trace of A is,

- (a) 17 (b) 25 (c) 8 (d) 15

15. If A is an orthogonal matrix, then

- (a) $|A| = 0$ (b) $|A| = \pm 1$
(c) $|A| = \pm 2$ (d) None of these.

16. If $A = \begin{bmatrix} 2 & -2 & -4 \\ -1 & 3 & 4 \\ 1 & -2 & x \end{bmatrix}$ is an idempotent matrix then $x =$

- (a) -5 (b) -1 (c) -3 (d) -4

17. If $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & -2 & 4 \end{bmatrix}$, $I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ and

$A^{-1} = \frac{1}{6}(A^2 + cA + d)$ then the values of c and d are

respectively -

- (a) -6, -11 (b) 6, 11 (c) -6, 11 (d) None of these

18. If $A = \begin{bmatrix} 0 & \alpha & \alpha \\ 2\beta & \beta & -\beta \\ \gamma & -\gamma & \gamma \end{bmatrix}$ is an orthogonal matrix, then the

number of possible triplets (α, β, γ)

- (a) 8 (b) 6 (c) 4 (d) 2



19. The number of solutions of the matrix equation

$$A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \text{ is -}$$

- (a) 2 (b) 4 (c) 8 (d) Infinitely many

20. If the matrix M_r is given by $M_r = \begin{bmatrix} r & r-1 \\ r-1 & r \end{bmatrix}$,

$r = 1, 2, 3, \dots$. Then the value of $\det(M_1) + \det(M_2) + \dots + \det(M_{2009})$ is

- (a) 2008 (b) 2009 (c) $(2009)^2$ (d) $(2008)^2$

21. If $\begin{bmatrix} \alpha & \beta \\ \gamma & -\alpha \end{bmatrix}$ is to be square root of two rowed unit matrix

then α, β and γ should satisfy the relation

- (a) $1 + \alpha^2 + \beta\gamma = 0$ (b) $1 - \alpha^2 - \beta\gamma = 0$
(c) $1 - \alpha^2 + \beta\gamma = 0$ (d) $\alpha^2 - \beta\gamma + 1 = 0$

22. If $A = \begin{bmatrix} 0 & -1 & 2 \\ 1 & 0 & 3 \\ -2 & -3 & 0 \end{bmatrix}$, then $A + 2A^T$ equals -

- (a) A (b) $-A^T$ (c) A^T (d) $2A^2$

23. If A is matrix of order 3 and $|A| = 2$, then $|\text{adj } A|$ is equal to .

- (a) 1 (b) 2 (c) 2^3 (d) 2^2

24. Matrix $[1 \ 2] \left(\begin{bmatrix} -2 & 5 \\ 3 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \end{bmatrix} \right)$ is equal to-

- (a) $[1 \ 2 \ 2]$ (b) $[2 \ 3]$ (c) $[2 \ 2]$ (d) None of these

25. If w is a complex cube root of unity, then the matrix $A =$

$$\begin{bmatrix} 1 & w^2 & w \\ w^2 & w & 1 \\ w & 1 & w^2 \end{bmatrix} \text{ is a-}$$

- (a) Singular matrix (b) Non-singular matrix
(c) Skew symmetric matrix (d) None of these